



**University of Stuttgart**  
Germany  
Institute for Sanitary Engineering,  
Water Quality and Solid Waste Management  
AQS Baden-Württemberg

**INTERNATIONAL  
STANDARD**

**ISO  
11352**

First edition  
2012-07-01

**Water quality — Estimation of  
measurement uncertainty based on  
validation and quality control data**

Excel tool for estimation  
of measurement  
uncertainty from  
validation and quality  
control according to ISO  
11352

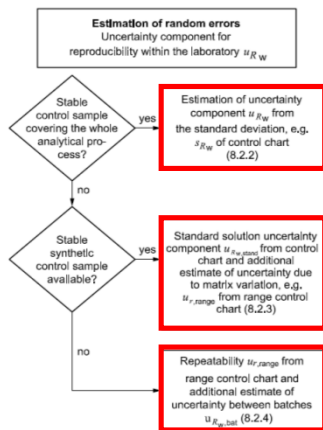
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## Principle of ISO 11352 and the NORDTEST technical report

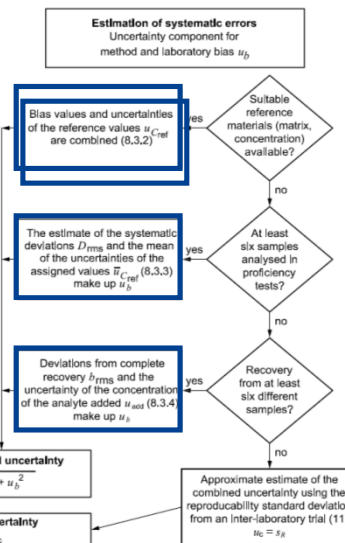


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### Precision



### Trueness



**Combined standard uncertainty**  
 $u_C = \sqrt{u_{R_W}^2 + u_b^2}$

**Expanded uncertainty**  
 $U = k \cdot u_C$

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## General

- The idea of these EXCEL® sheets is to fully reflect the ISO standard ISO 11352
- Their design is intended to allow not only the estimation, but also use it for documentation

	A	B	C	D	E	F	G	H
1	<b>Estimation of measurement uncertainty</b>							v2.31 rel
2	for the determination of							
3	in							
4	using							
5	for the concentration range:							
6	on the basis of							
7	ISO DIS 11352:2010 Water quality — Determination of measurement uncertainty based on							
8	validation data							
9								
10	calculated by:							
11	Date:			Signature:				
12								
13	<b>Reproducibility within Laboratory</b>				<b><math>U_{Rw}</math></b>			
14	No.	contribution				rel. standard uncertainty		
15	1							
16	2							
17	3							
18	<b>Combined uncertainty component</b>				<b><math>U_{Rw}</math></b>			
19	<b>Method and Laboratory Bias</b>				<b><math>U_{bias}</math></b>			
20	No.	contribution				rel. standard uncertainty		
21	1							
22	2							
23	3							
24	<b>Combined uncertainty component</b>				<b><math>U_{bias}</math></b>			
25	<b>Total Combined Standard uncertainty u</b>							
26	<b>Expanded Uncertainty U</b>				<b>k-factor</b>			
27	© 2015 Dr. M. Koch, Institute for Sanitary Engineering, Universität Stuttgart, www.aqsbw.de							
28	The use of this EXCEL-sheet is free, as long as the copyright statement is not removed.							
		total	reproducibility	method and laboratory bias	s from range	m and s from data	combination	

Sheet  
„total“



# Sheet „total“

	A	B	C	D	E	F	G	H
1	<b>Estimation of measurement uncertainty</b> v2.31 rel							
2	for the determination of	mass concentration of Cd						
3	in	aqua regia extract of soil						
4	using	microwave digestion and ICP-OES						
5	for the concentration range:	X to Y mg/l						
6	on the basis of							
7	ISO DIS 11352:2010 Water quality — Determination of measurement uncertainty based on							
8	validation data							
9								
10	calculated by	John Smith			Signature: <input type="text"/>			
11	Date:	05 Jan 2019						
12								
13	<b>Reproducibility within Laboratory</b>				<b><math>U_{Rw}</math></b>			
14	No.	contribution			rel. standard uncertainty			
15	1	X-Chart 03-178			5,46%			
16	2							
17	3							
18	<b>Combined uncertainty component</b>				<b><math>U_{Rw}</math></b>		<b>5,46%</b>	
19	<b>Method and Laboratory Bias</b>				<b><math>U_{bias}</math></b>			
20	No.	contribution			rel. standard uncertainty			
21	1	CRM BCR-142R			3,15%			
22	2							
23	3							
24	<b>Combined uncertainty component</b>				<b><math>U_{bias}</math></b>		<b>3,15%</b>	
25	<b>Total Combined Standard uncertainty u</b>				<b>6,30%</b>			
26	<b>Expanded Uncertainty U</b>				<b>k-factor</b>		<b>2</b>	
27	© 2015 Dr. M. Koch, Institute for Sanitary Engineering, Universität Stuttgart, www.aqsbw.de							
28	The use of this EXCEL-sheet is free, as long as the copyright statement is not removed.							
		total	reproducibility	method and laboratory bias	s from range	m and s from data	combination	

# Sheet „reproducibility“

	A	B	C	D	E	F	G	H	I	J	K
1	<b>Reproducibility within laboratory</b> <b><math>U_{Rw}</math></b>										
2	<b>A) Control sample, covering the whole analytical process</b>										
3	Standard deviation: <input type="text"/>										
4	at concentration: <input type="text"/>										
5	rel standard deviation: <input type="text"/> transfer to sheet "Total"										
6											
7	Remarks: <input type="text"/>										
8											
9											
10	<b>B) Control sample, not covering the whole analytical process</b>										
11	B.1 result from the control sample										
12	Standard deviation: <input type="text"/>										
13	at concentration: <input type="text"/>										
14	rel standard deviation: <input type="text"/>										
15	B.2 component from changing matrices and concentrations (from range)										
16	Mean rel. range: <input type="text"/> sheet "s from range", cell M4										
17	Number of measurements for the range (2, 3, 4 or 5) <input type="text"/>										
18	rel. standard deviation: <input type="text"/>										
19	Combination: <input type="text"/> transfer to sheet "Total"										
20											
21	Remarks: <input type="text"/>										
22											
23											
24	<b>C) Unstable control samples</b>										
25	C.1 Repeatability										
26	Mean rel. range: <input type="text"/> sheet "s from range", cell M4										
27	Number of measurements for the range (2, 3, 4 or 5) <input type="text"/>										
28	Standard deviation: <input type="text"/>										
29	C.2 "Long term" component										
30	Estimation for standard deviation <input type="text"/>										
31	based on <input type="text"/>										
32	Combination: <input type="text"/> transfer to sheet "Total"										
33											
34	Remarks: <input type="text"/>										
35											

In this sheet three approaches are given to quantify the uncertainty contribution caused by the imprecision. Please choose the most appropriate one.  
For more details see ISO DIS 11352:2010 Water quality — Determination of measurement uncertainty based on validation data.

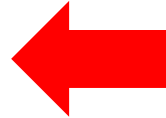
# Sheet „reproducibility“



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	A	B	C	D	E	F	G	H	I	J	K
1	<b>Reproducibility within laboratory</b> $U_{Rw}$										
2	<b>A) Control sample, covering the whole analytical process</b>										
3	Standard deviation:		0,04								
4	at concentration:		0,41								
5	rel standard deviation:		9,76%								transfer to sheet "Total"
6											
7	Remarks:	30 results from X-Chart 03-178 Jul-Dec 2018									
8											
9											
10	<b>B) Control sample, not covering the whole analytical process</b>										
11	B.1 result from the control sample										
12	Standard deviation:										
13	at concentration:										
14	rel standard deviation:										
15	B.2 component from changing matrices and concentrations (from range)										
16	Mean rel. range:										sheet "s from range", cell M4
17	Number of measurements for the range (2, 3, 4 or 5)										
18	rel. standard deviation:										
19	Combination:										transfer to sheet "Total"
20											
21	Remarks:										
22											
23											
24	<b>C) Unstable control samples</b>										
25	C.1 Repeatability										
26	Mean rel. range:										sheet "s from range", cell M4
27	Number of measurements for the range (2, 3, 4 or 5)										
28	Standard deviation:										
29	C.2 "Long term" component										
30	Estimation for standard deviation										
31	based on										
32	Combination:										transfer to sheet "Total"
33											
34	Remarks:										
35											

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For more details see ISO DIS 11352:2010 Water quality — Determination of measurement uncertainty based on validation data.



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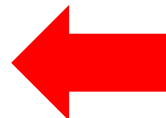
# Sheet „reproducibility“



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	A	B	C	D	E	F	G	H	I	J	K
1	<b>Reproducibility within laboratory</b> $U_{Rw}$										
2	<b>A) Control sample, covering the whole analytical process</b>										
3	Standard deviation:										
4	at concentration:										
5	rel standard deviation:										transfer to sheet "Total"
6											
7	Remarks:										
8											
9											
10	<b>B) Control sample, not covering the whole analytical process</b>										
11	B.1 result from the control sample										
12	Standard deviation:		0,45								
13	at concentration:		19,5								
14	rel standard deviation:		2,31%								
15	B.2 component from changing matrices and concentrations (from range)										
16	Mean rel. range:				5,61%						sheet "s from range", cell M4
17	Number of measurements for the range (2, 3, 4 or 5)				2						
18	rel. standard deviation:				4,97%						
19	Combination:				5,48%						transfer to sheet "Total"
20											
21	Remarks:	30 results X-Chart 03-178 Jul-Dec 2018 / 50 results from, R-Chart 01-143 2018									
22											
23											
24	<b>C) Unstable control samples</b>										
25	C.1 Repeatability										
26	Mean rel. range:										sheet "s from range", cell M4
27	Number of measurements for the range (2, 3, 4 or 5)										
28	Standard deviation:										
29	C.2 "Long term" component										
30	Estimation for standard deviation										
31	based on										
32	Combination:										transfer to sheet "Total"
33											
34	Remarks:										
35											

In this sheet three approaches are given to quantify the uncertainty contribution caused by the imprecision. Please choose the most appropriate one.  
For more details see ISO DIS 11352:2010 Water quality — Determination of measurement uncertainty based on validation data.



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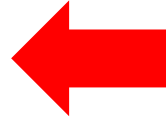
# Sheet „reproducibility“



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1	<b>Reproducibility within laboratory</b>				$U_{RW}$	
2	<b>A) Control sample, covering the whole analytical process</b>					
3	Standard deviation:					
4	at concentration:					
5	rel standard deviation: <input type="text"/> transfer to sheet "Total"					
6	Remarks:					
7						
8						
9						
10	<b>B) Control sample, not covering the whole analytical process</b>					
11	B.1 result from the control sample					
12	Standard deviation:					
13	at concentration:					
14	rel standard deviation: <input type="text"/>					
15	B.2 component from changing matrices and concentrations (from range)					
16	Mean rel. range: <input type="text"/> sheet "s from range", cell M4					
17	Number of measurements for the range (2, 3, 4 or 5)					
18	rel. standard deviation: <input type="text"/>					
19	Combination: <input type="text"/> transfer to sheet "Total"					
20	Remarks:					
21						
22						
23						
24	<b>C) Unstable control samples</b>					
25	C.1 Repeatability					
26	Mean rel. range: <input type="text"/> 2,13% sheet "s from range", cell M4					
27	Number of measurements for the range (2, 3, 4 or 5) <input type="text"/> 2					
28	Standard deviation: <input type="text"/> 1,89%					
29	C.2 "Long term" component					
30	Estimation for standard deviation <input type="text"/> 0,5%					
31	based on <input type="text"/> Observed variations in the daily calibration					
32	Combination: <input type="text"/> 1,95% transfer to sheet "Total"					
33	Remarks:					
34	50 results from, R-Chart 01-143 2018					
35						

In this sheet three approaches are given to quantify the uncertainty contribution caused by the imprecision. Please choose the most appropriate one.  
For more details see ISO DIS 11352:2010 Water quality — Determination of measurement uncertainty based on validation data.



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1	<b>Method and Laboratory Bias</b>				$U_{MB}$	
2	<b>1) Method and Laboratory Bias</b>					
3	Standard deviation:					
4	at concentration:					
5	rel standard deviation: <input type="text"/>					
6	Remarks:					
7						
8						
9						
10	<b>2) Multiple analysis of material samples of reference substances</b>					
11	Mean result:					
12	Standard deviation:					
13	rel standard deviation: <input type="text"/>					
14	Remarks:					
15						
16						
17						
18						
19						
20						
21						
22						
23						
24						
25						
26						
27						
28						
29						
30						
31						
32						
33						
34						
35						

1 CRM

several CRMs

PT results

Recovery experiments



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# Sheet „method and laboratory bias“

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# Sheet „method and laboratory bias“ CRM part

	A	B	C	D	E	F	G	H	I	J	K
1	<b>Method and Laboratory Bias</b>				<b>U<sub>bias</sub></b>						
2	<b>A) Multiple Analysis of one certified reference material</b>										
3	Certified value		unit:		Remarks:						
4	Confidence interval +/-										
5	Confidence level										
6	Relative Standard uncertainty:										
7	Mean of CRM-analysis:										
8	Mean deviation:										
9	Mean deviation in %										
10	Std.-deviation of CRM-analysis:										
11	rel. std.-deviation of CRM-analysis:										
12	Number of measurements:										
13	Standard uncertainty					transfer to sheet "Total"					
14											
15	<b>B) Multiple analysis of several certified reference materials</b>										
16		cert. value	confid. interval	confid. level	mean	Remarks:					
17	CRM 1										
18	CRM 2										
19	CRM 3										
20	CRM 4										
21		u(C <sub>ref</sub> )		deviation	squared dev.						
22	CRM 1										
23	CRM 2										
24	CRM 3										
25	CRM 4										
26	mean		RMS <sub>bias</sub>								
27	Standard uncertainty					transfer to sheet "Total"					

In this sheet four approaches are given to quantify the uncertainty contribution caused by the method and laboratory bias. Please choose the most appropriate one.

For more details see ISO DIS 11352:2010 Water quality — Determination of measurement uncertainty based on validation data.



# Sheet „method and laboratory bias“ CRM part

	A	B	C	D	E	F	G	H	I	J	K
1	<b>Method and Laboratory Bias</b>				<b>U<sub>bias</sub></b>						
2	<b>A) Multiple Analysis of one certified reference material</b>										
3	Certified value	0,249	unit:	mg/kg	Remarks:	10 measurements of BCR 142R in 2018					
4	Confidence interval +/-	0,01									
5	Confidence level	95%									
6	Relative Standard uncertainty:			2,05%							
7	Mean of CRM-analysis:			0,2337	mg/kg						
8	Mean deviation:			-0,0153							
9	Mean deviation in %			-6,14%							
10	Std.-deviation of CRM-analysis:			0,0112	mg/kg						
11	rel. std.-deviation of CRM-analysis:			4,79%							
12	Number of measurements:			10							
13	Standard uncertainty			6,65%		transfer to sheet "Total"					
14											
15	<b>B) Multiple analysis of several certified reference materials</b>										
16		cert. value	confid. interval	confid. level	mean	Remarks:					
17	CRM 1										
18	CRM 2										
19	CRM 3										
20	CRM 4										
21		u(C <sub>ref</sub> )		deviation	squared dev.						
22	CRM 1										
23	CRM 2										
24	CRM 3										
25	CRM 4										
26	mean		RMS <sub>bias</sub>								
27	Standard uncertainty					transfer to sheet "Total"					

In this sheet four approaches are given to quantify the uncertainty contribution caused by the method and laboratory bias. Please choose the most appropriate one.

For more details see ISO DIS 11352:2010 Water quality — Determination of measurement uncertainty based on validation data.





# Sheet „method and laboratory bias“ CRM part

	A	B	C	D	E	F	G	H	I	J	K
1	<b>Method and Laboratory Bias</b>				<b>U<sub>bias</sub></b>						
2	<b>A) Multiple Analysis of one certified reference material</b>										
3	Certified value	unit:		Remarks:							
4	Confidence interval +/-										
5	Confidence level										
6	Relative Standard uncertainty:										
7	Mean of CRM-analysis:										
8	Mean deviation:										
9	Mean deviation in %										
10	Std.-deviation of CRM-analysis:										
11	rel. std.-deviation of CRM-analysis:										
12	Number of measurements:										
13	Standard uncertainty			transfer to sheet "Total"							
14											
15	<b>B) Multiple analysis of several certified reference materials</b>										
16		cert. value	confid. interval	confid. level	mean	Remarks:					
17	CRM 1	11,5	0,5	95%	11,9	10 measurements of BCR 142R in 2018					
18	CRM 2	22,6	0,8	95%	22,4	15 measurements of FTZ 364 in 2018					
19	CRM 3	34,3	1,0	95%	35,2	12 measurements of JTU 284 in 2018					
20	CRM 4										
21		u(C <sub>ref</sub> )		deviation	squared dev.						
22	CRM 1	2,22%		3,48%	0,0012						
23	CRM 2	1,81%		-0,88%	0,0001						
24	CRM 3	1,49%		2,62%	0,0007						
25	CRM 4										
26	mean	1,84%	RMS <sub>bias</sub>	2,57%							
27	Standard uncertainty	3,16%				transfer to sheet "Total"					



# Sheet „method and laboratory bias“ PT part

	A	B	C	D	E	F	G	H	I	J	K
28											
29	<b>C) Proficiency tests</b>										
30	<b>Own results</b>										
31		Assigned val.	result	deviation	squared deviation	Remarks:					
32	Sample 1										
33	Sample 2										
34	Sample 3										
35	Sample 4										
36	Sample 5										
37	Sample 6										
38	Sample 7										
39	Sample 8										
40	Sample 9										
41	Sample 10										
42	Sample 11										
43	Sample 12										
44				RMS <sub>bias</sub>							
45	<b>Uncertainty of the assigned value</b>										
46	consensus mean					Information from PT provider					
47	<input checked="" type="radio"/> robust mean <input type="radio"/> arithmetic mean										
48	SR (%)	N values	u(C <sub>ref</sub> )	Unc. in % Conf-level u(C <sub>ref</sub> )							
49	Sample 1										
50	Sample 2										
51	Sample 3										
52	Sample 4										
53	Sample 5										
54	Sample 6										
55	Sample 7										
56	Sample 8										
57	Sample 9										
58	Sample 10										
59	Sample 11										
60	Sample 12										
61		mean				mean					
62											
63	Standard uncertainty										transfer to sheet "Total"





# Sheet „method and laboratory bias“ PT part

	A	B	C	D	E	F	G	H	I	J	K
28											
29	C) Proficiency tests										
30	Own results										
31		Assigned val.	result	deviation	squared deviation	Remarks:					
32	Sample 1	7,532	7,47	-0,82%	0,000068	AQS BW waste water PTs 14. LURV and 19. LURV					
33	Sample 2	28,31	28,2	-0,39%	0,000015						
34	Sample 3	37,67	37,4	-0,72%	0,000051						
35	Sample 4	7,967	8,18	2,67%	0,000715						
36	Sample 5	13,58	13,5	-0,59%	0,000035						
37	Sample 6	35,73	35,8	0,20%	0,000004						
38	Sample 7										
39	Sample 8										
40	Sample 9										
41	Sample 10										
42	Sample 11										
43	Sample 12										
44				RMS <sub>bias</sub>							
45	Uncertainty of the assigned value										
46	consensus mean						Information from PT provider				
47	<input checked="" type="radio"/> robust mean <input type="radio"/> arithmetic mean										
48		sr (%)	N values	u(C <sub>ref</sub> )		Unc. in %	Conf-level	u(C <sub>ref</sub> )			
49	Sample 1	3,42%	62	0,54%							
50	Sample 2	3,62%	61	0,58%							
51	Sample 3	3,93%	62	0,62%							
52	Sample 4	5,29%	37	1,09%							
53	Sample 5	5,10%	37	1,05%							
54	Sample 6	5,05%	36	1,04%							
55	Sample 7										
56	Sample 8										
57	Sample 9										
58	Sample 10										
59	Sample 11										
60	Sample 12										
61			mean	0,82%				mean			
62	Standard uncertainty		1,47%	transfer to sheet "Total"							



# Sheet „method and laboratory bias“ Recovery experiment part

	A	B	C	D	E	F	G	H	I	J	K
64											
65	D) Recovery Experiment										
66	Uncertainty of the concentration of the spike solution:										
67	Concentration of the spike solution:										
68	Confidence interval +/-										
69	Confidence level:										
70	U <sub>conc</sub>										
71	Uncertainty of the added volume:										
72	max. deviation [%] (rectangular distribution)										
73	Repeatability [%] (as standard deviation)										
74	U <sub>vol</sub>										
75	Uncertainty of the spike:										
76	Recovery:										
77		spike	found	recovery	rel. deviation	squared rel. deviation	Remarks:				
78	1										
79	2										
80	3										
81	4										
82	5										
83	6										
84	7										
85	8										
86	9										
87	10										
88	11										
89	12										
90					RMS <sub>bias</sub>						
91	Standard uncertainty				transfer to sheet "Total"						



# Sheet „method and laboratory bias“ Recovery experiment part

	A	B	C	D	E	F	G	H	I	J	K
64											
65	<b>D) Recovery Experiment</b>										
66	<b>Uncertainty of the concentration of the spike solution:</b>										
67	Concentration of the spike solution:			125							
68	Confidence interval +/-			0,82							
69	Confidence level:			1 s							
70	$U_{conc}$			0,66%							
71	<b>Uncertainty of the added volume:</b>										
72	max. deviation [%] (rectangular distribution)			1,00%	Std-dev.:	0,58%					
73	Repeatability [%] (as standard deviation)										
74	$U_{vol}$			0,64%							
75	<b>Uncertainty of the spike:</b>										
76	$U_{spike}$			0,91%							
77	<b>Recovery:</b>										
78		spike	found	recovery	rel. deviation	squared rel. deviation					
79	1	94,2	100,1	106,26%	6,26%	0,39%	Remarks:				
80	2	94,2	89,5	95,01%	-4,99%	0,25%					
81	3	94,2	103,3	109,66%	9,66%	0,93%					
82	4	94,2	101,3	107,54%	7,54%	0,57%					
83	5	94,2	90,4	95,97%	-4,03%	0,16%					
84	6	94,2	97,8	103,82%	3,82%	0,15%					
85	7	94,2	93	98,73%	-1,27%	0,02%					
86	8	94,2	88	93,24%	-6,58%	0,43%					
87	9	94,2	88,8	94,27%	-5,73%	0,33%					
88	10	94,2	100,1	100,85%	0,85%	0,01%					
89	11										
90							RMS <sub>bias</sub>	5,69%			
91	Standard uncertainty			5,76%	transfer to sheet "Total"						

# Support-sheet „m and s from data“

	A	B	C	D	E
1		values			
2	1		mean:		
3	2		standard deviation		
4	3		rel. standard deviation		
5	4				
6	5				
7	6		Remarks:		
8	7				
9	8				
10	9				
11	10				
12	11				
13	12				
14	13				
15	14				
16	15				
17	16				
18	17				
19	18				
20	19				
21	20				
22	21				
23	22				
24	23				
25	24				
26	25				
27	26				
28	27				
29	28				
30	29				
31	30				
32	31				
33	32				
34	33				
35	34				

This sheet is a tool to calculate the arithmetic mean and the standard deviation from a data set.  
If you need more than one calculation of this kind just copy the whole sheet "m and s from data"

# Support-sheet „m and s from data“

	A	B	C	D	E
1		values			
2	1	0.49	mean:	0.501	
3	2	0.5	standard deviation	0.019119507	
4	3	0.52	rel. standard deviation	3.816%	
5	4	0.48			
6	5	0.49			
7	6	0.51	Remarks:	Data from X-chart 354-34 from Jan to Jul 19	
8	7	0.51			
9	8	0.54			
10	9	0.48			
11	10	0.49			
12	11				
13	12				
14	13				
15	14				
16	15				
17	16				
18	17				
19	18				
20	19				
21	20				
22	21				
23	22				
24	23				
25	24				
26	25				
27	26				
28	27				
29	28				
30	29				
31	30				
32	31				
33	32				
34	33				
35	34				

This sheet is a tool to calculate the arithmetic mean and the standard deviation from a data set.  
If you need more than one calculation of this kind just copy the whole sheet "m and s from data"

# Support-sheet „s from range“

	A	B	C	D	E	F	G	H	I	J	K	L	M	N
1		1st value	2nd value	3rd value	4th value	5th value			mean	range	rel. range			
2	1						number of measurem.					total mean		
3	2						s (absolute)					mean range		
4	3						s (relative)					mean rel. range		
5	4													
6	5													
7	6													
8	7													
9	8													
10	9													
11	10													
12	11													
13	12													
14	13													
15	14													
16	15													
17	16													
18	17													
19	18													
20	19													
21	20													
22	21													
23	22													
24	23													
25	24													
26	25													
27	26													
28	27													
29	28													
30	29													
31	30													
32	31													
33	32													

This sheet is a tool to calculate a repeatability standard deviation (cells H3 and H4 resp.) from the mean of ranges (e.g. from a range control chart). The "mean rel. range" (cell M4) is needed for the calculation of the repeatability part of the uncertainty in sheet "reproducibility" (cells E13 or E20).  
If you need more than one calculation of this kind just copy the whole sheet "s from range"



# Support-sheet „s from range“

	A	B	C	D	E	F	G	H	I	J	K	L	M	N
1														
2	1	18,3	18,4				number of measurem.	2	18,35	0,1	0,54%	total mean	20,428	
3	2	25,3	24,6				s (absolute)	0,9707447	24,95	0,7	2,81%	mean range	1,095	
4	3	15,2	16,2				s (relative)	4,97%	15,7	1	6,37%	mean rel. range	5,8113%	
5	4	32,3	32,1						32,2	0,2	0,62%			
6	5	14,4	15,6						15	1,2	8,00%	Remarks:		
7	6	20,1	21,8						20,95	1,7	8,11%	Ranges from range		
8	7	15,3	16,1						15,7	0,8	5,10%	chart R25/12 from		
9	8	14,8	15,6						15,2	0,8	5,26%	Jan to Jul 2019		
10	9	19,9	20,8						20,35	0,9	4,42%			
11	10	32,1	33,2						32,65	1,1	3,37%			
12	11	16,5	18,6						17,55	2,1	11,97%			
13	12	17,1	19,3						18,2	2,2	12,09%			
14	13	20,1	20,2						20,15	0,1	0,50%			
15	14	11,3	12,1						11,7	0,8	6,84%			
16	15	18,7	18,8						18,75	0,1	0,53%			
17	16	19,2	19,2						19,2	0	0,00%			
18	17	21,3	21,6						21,45	0,3	1,40%			
19	18	27,3	29,1						28,2	1,8	6,38%			
20	19	29,1	25,1						27,1	4	14,76%			
21	20	14,2	16,2						15,2	2	13,16%			
22	21													
23	22													
24	23													
25	24													
26	25													
27	26													
28	27													
29	28													
30	29													
31	30													
32	31													
33	32													

This sheet is a tool to calculate a repeatability standard deviation (cells H3 and H4 resp.) from the mean of ranges (e.g. from a range control chart). The "mean rel. range" (cell M4) is needed for the calculation of the repeatability part of the uncertainty in sheet "reproducibility" (cells E13 or E20).

If you need more than one calculation of this kind just copy the whole sheet "s from range"

Remarks:  
Ranges from range chart R25/12 from Jan to Jul 2019



# Support-sheet „combination“

	A	B	C	D	E	F	G	H	I	J	K
1											
2											
3	No.	description	deviation	confidence level	denominator	u					
4	1										
5	2										
6	3										
7	4										
8	5										
9	6										
10	7										
11	8										
12	9										
13	10										
14											
15											
16	No.	description	deviation	confidence level	denominator	u					
17	1										
18	2										
19	3										
20	4										
21	5										
22	6										
23	7										
24	8										
25	9										
26	10										
27											
28											

With this sheet you may calculate standard deviations (standard uncertainty components) from other measures of dispersion, namely the half width of

- 95% confidence interval
- 2 standard deviations
- 99% confidence interval
- 3 standard deviations
- rectangular distribution
- triangular distribution

and combines according to the law of error (uncertainty) propagation.

$$U_c = \sqrt{U_1^2 + U_2^2 + \dots + U_n^2}$$

If this sheet is not sufficient for your calculations, just copy the whole sheet "combination"



## Support-sheet „combination“

No.	description	deviation	confidence level	denominator	u
1	Measuring flask 1, bias	0,200%	rectangle	1,732	0,115%
2	Measuring flask 2, bias	0,200%	rectangle	1,732	0,115%
3	Measuring flask 3, bias	0,200%	rectangle	1,732	0,115%
4	Pipette 1, bias	0,700%	rectangle	1,732	0,404%
5	Pipette 2, bias	0,700%	rectangle	1,732	0,404%
6	Measuring flask 1, prec.	0,045%	1 s	1	0,045%
7	Measuring flask 2, prec.	0,045%	1 s	1	0,045%
8	Measuring flask 3, prec.	0,045%	1 s	1	0,045%
9	Pipette 1, prec.	0,140%	1 s	1	0,140%
10	Pipette 2, prec.	0,140%	1 s	1	0,140%
				combination	0,642%

With this sheet you may calculate standard deviations (standard uncertainty components) from other measures of dispersion, namely the half width of  
- 95% confidence interval  
- 2 standard deviations  
- 99% confidence interval  
- 3 standard deviations  
- rectangular distribution  
- triangular distribution  
and combine according to the law of error (uncertainty) propagation.

$$u_c = \sqrt{u_1^2 + u_2^2 + \dots + u_n^2}$$

If this sheet is not sufficient for your calculations, just copy the whole sheet "combination"



## Availability

- The Excel sheets are available from
  - [www.aqsbw.de/en](http://www.aqsbw.de/en) -> download -> software  
-> freeware programmes in English
  - [www.aqsbw.de](http://www.aqsbw.de) -> Download -> Software  
-> Freeware-Programme in German
- Thank you for your attention