





**Measurement uncertainty in R:
The metRology package**

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Introduction

- What is R?
- What is the metRology package?
- Functionality: What does it do?
- Philosophy: Who owns it?
- Location: Where is it?



What is ...



- R
 - “R is an integrated suite of software facilities for data manipulation, calculation and graphical display”
 - Free, open source package for statistical analysis and programming
 - Extensible via “packages”
- The metRology package
 - An R package for statistics applied to metrology
 - metrology: The science of measurement



Functionality: What does it do?



“metRology provides classes and calculation and plotting functions for metrology applications, including measurement uncertainty estimation and inter-laboratory metrology comparison studies.”

<https://r-forge.r-project.org/projects/metrology/>

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- Measurement uncertainty estimation
- Support for interlaboratory studies



metRology: Functions



Application area			
	Measurement uncertainty	Inter-laboratory study	Ancillary
Functions	Construct uncertainty budgets: <i>Algebraic,</i> <i>Numerical: <code>uncert()</code></i> <i>Monte Carlo: <code>uncertMC()</code></i> Explore uncertainty budgets: <i><code>print()</code>, <code>plot()</code></i> <i><code>drop1()</code>, <code>update()</code></i> <i><code>contribs()</code></i>	Review data: <i><code>kplot()</code></i> <i><code>cplot()</code></i> <i><code>duewer.plot()</code></i> Check data: <i><code>msd()</code></i> Form estimates: <i><code>mpaule()</code></i> <i><code>huber.estimate()</code></i> <i><code>MM.estimate()</code></i> <i><code>labGRE()</code> ...</i>	<i><code>w.s()</code>, <code>ptri()</code></i> <i><code>buildCor()</code></i> <i><code>buildCov()</code></i>

Measurement uncertainty



1. ISO Guide to the Expression of Uncertainty in Measurement

- First-order error propagation from a 'measurement model'

$$y = f(x_1, x_2, \dots, x_n)$$

$$u(y) = \sqrt{\sum_{i=1}^n \left(\frac{\partial y}{\partial x_i} u(x_i) \right)^2 + 2 \sum_{i=1}^n \sum_{j>i}^n \frac{\partial y}{\partial x_i} \frac{\partial y}{\partial x_j} \text{cov}(x_i, x_j)}$$

- Correlation allowed for



Uncertainty implementations in metRology



- Direct combination of contributions $u_i(y) = u(x_i) \frac{\partial y}{\partial x_i}$
- Algebraic differentiation of $f(x_1, \dots)$
- Numerical differentiation
 - Kragten's method

$$u(x_i) \partial y / \partial x_i \approx f(x_i + u(x_i)) - f(x_i)$$
 - Symmetric finite difference

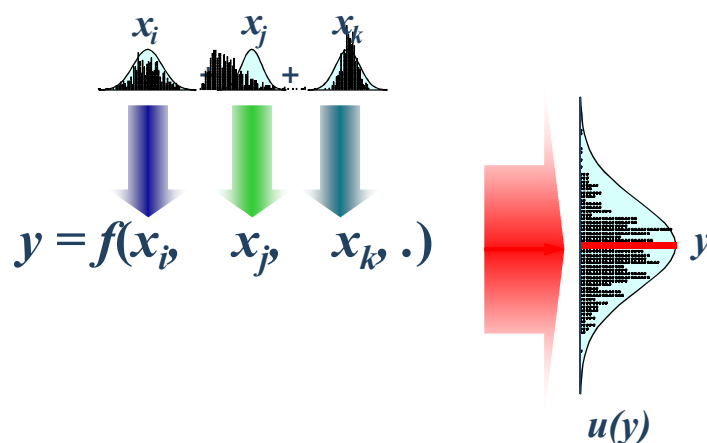
$$\partial y / \partial x_i \approx [f(x_i + \delta x_i) - f(x_i - \delta x_i)] / 2 \delta x_i$$



Uncertainty implementations in metRology



2. Monte Carlo (GUM Supplement 1)



Examples



```
expr <- expression(a+b*2+c*3+d/2)
# a=1(0.1), b=3(0.3), c=2(0.2), d=11(1.1)
u.expr<-uncert(expr, x, u, method="NUM")
```

```
#Compare with default:
uncert(u=c(0.1, 0.3, 0.2, 1.1), c=c(1.0, 2.0, 3.0,
0.5))
```

```
#... or with function method
f <- function(a,b,c,d) a+b*2+c*3+d/2
u.fun<-uncert(f, x, u, method="NUM")
```

```
#.. or with the formula method
u.form<-uncert(~a+b*2+c*3+d/2, x, u, method="NUM")
```



Examples (cont.)



Uncertainty evaluation

Call:

```
uncert.expression(expr = expr, x = x, u = u, method =
"NUM")
```

Expression: $a + b * 2 + c * 3 + d/2$

Evaluation method: NUM

Uncertainty budget:

	x	u	c	u.c
a	1	0.1	1.0	0.10
b	3	0.3	2.0	0.60
c	2	0.2	3.0	0.60
d	11	1.1	0.5	0.55

y:	18.5
u(y):	1.01612



A more interesting Monte carlo case



```
expr <- expression(a/(b-c))
x <- list(a=1, b=3, c=2)
Expression: a/(b - c)
```

```
      y: 1
E[u(y)]: 0.2187031
```

Monte Carlo evaluation using 999 replicates:

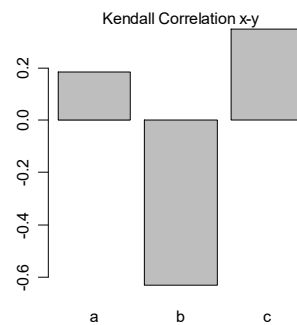
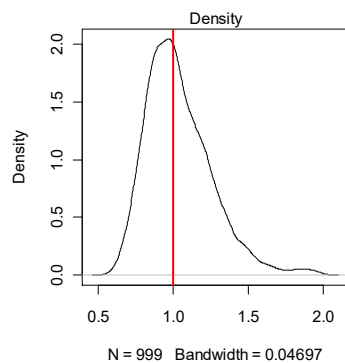
```
      y:
a      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
b      0.6047  0.8845  1.0020  1.0410  1.1630  1.9540
c
```



A more interesting Monte carlo case



```
> par(mfrow=c(2,2))
> plot(u.invexpr, which=1:4, pch=20, method="k")
# method="k" gives Kendall correlation
```



Other MU diagnostics and utilities



```
#An example with correlation
> u.cor<-diag(1,4)
> u.cor[3,4]<-u.cor[4,3]<-0.5
> u.formc<-uncert(~a+b*2+c*3+d/2, x, u, method="NUM")
+ #Which uncertainties matter most?
> par(mfrow=c(2,2))
> plot(u.formc)
```

Builds a correlation matrix

Plots for exploring uncertainty budgets

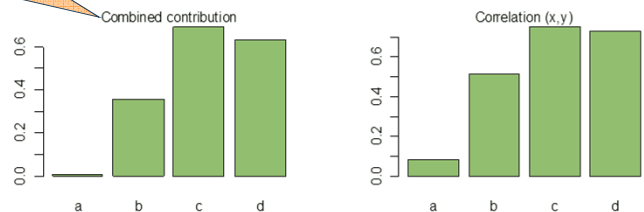


Other MU diagnostics and utilities: plot.uncert



Sum of all relevant covariance terms

Significant covariance included automatically



Other MU diagnostics and utilities

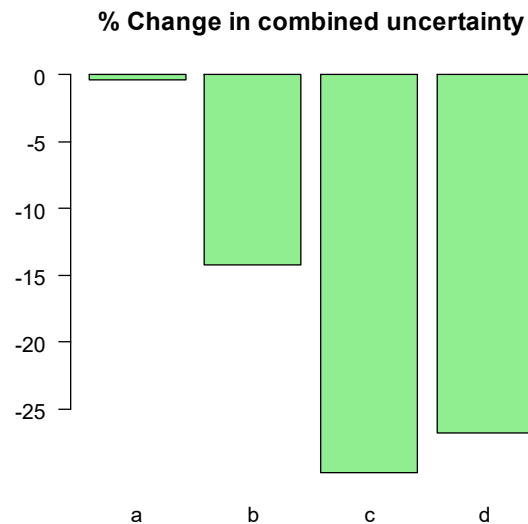


```
#An example with correlation
> u.cor<-diag(1,4)
> u.cor[3,4]<-u.cor[4,3]<-0.5
> u.formc<-uncert(~a+b*2+c*3+d/2, x, u, method="NUM")
+ #Which uncertainties matter most?
> par(mfrow=c(2,2))
> plot(u.formc)
```

```
#What happens if we reduce one uncertainty? Drop each term successively
> barplot(drop1(u.formc))
```



Other MU diagnostics and utilities: drop1



Other MU diagnostics and utilities



- update
 - Modifies uncertainty budgets (for example, changing an individual uncertainty or the method of evaluation)
- w.s, welch.satterthwaite
 - Welch-Satterthwaite effective degrees of freedom
- buildCov, buildCor
 - simplifies assembly of correlation or covariance matrices by taking a short list of labelled off-diagonal terms



Philosophy: Who owns metRology?



- metRology is an open source project
- No single 'owner'
- Contributions invited
- Licence is GPL
 - Copyright is held by code contributor
 - Contribution is conditional on granting full permissions under the GPL:
 - right to distribute and modify under the same terms



Location: Where is metRology?



- CRAN:
`install.packages("metRology")`
- R-Forge: metRology
<https://r-forge.r-project.org/projects/metrology/>
- Code access via SubVersion (svn)
 - Tortoise SVN for Windows



Acknowledgements



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